Churches and Local Economies

Zane Kashner Stanford GSB Max Pienkny Northwestern

August 6, 2025

Religion in the US

Religion has long been a major social institution in the United States

- 90% of US identified as Christian in the 1990s [Pew 2022]
- Now 63% do \rightarrow shift to unaffiliated

Religious institutions:

- 1. Integral to system of belief
- 2. Center of social support, communal identity, and civic life

Founding of US \rightarrow emphasis on religious liberty and pluralism

- Diverse religious landscape
- Two largest Christian orgs. in US: Catholic Church and Southern Baptist Convention

The Southern Baptist Convention

Evangelical Christian denomination

- Separated from National Convention in 1845
- Stemmed from disputes over slavery

Membership peaked at 16 million in 2006

- ↓ in membership since

40,000+ congregations throughout US

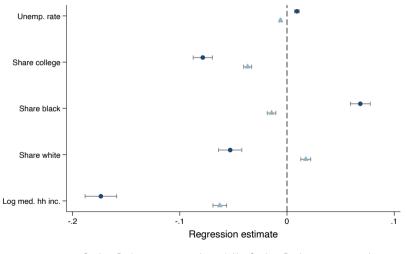
- Churches are fully autonomous & independent
- ightarrow diff. SBC churches imperfect substitutes



A Southern Baptist Church

Area characteristics and church presence

SBC church presence \rightarrow negative selection on all economic indicators



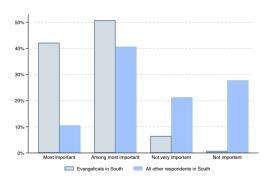
Southern Bapist congreg. per capita

Non-Southern Baptist congreg. per capita

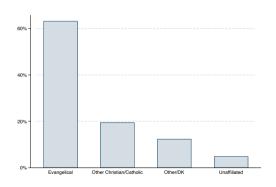
The SBC church in American life

Over 40% of SBC adherents say religion most important part of life (90+% among most)

- Social networks very segregated by religion



(a) Religious importance



(b) Friend composition

What is the causal role of religion for economic & social outcomes?

- Square personal importance with negative selection

What is the causal role of religion for economic & social outcomes?

- Square personal importance with negative selection

Exploit local "religion shocks" in the SBC to answer:

1. How do communities respond to religious shocks?

What is the *causal* role of religion for economic & social outcomes?

- Square personal importance with negative selection

Exploit local "religion shocks" in the SBC to answer:

- 1. How do communities respond to religious shocks?
- 2. How do religious changes affect outcomes?

What is the *causal* role of religion for economic & social outcomes?

- Square personal importance with negative selection

Exploit local "religion shocks" in the SBC to answer:

- 1. How do communities respond to religious shocks?
- 2. How do religious changes affect outcomes?
- 3. What is the role of religion & social connection as place-based amenities?

Explore in two ways:

Explore in two ways:

1. Pastor deaths

- SBC churches use single pastor for leadership
- 1-1 mapping from pastor deaths to church closures
- Pastor deaths o supply shifter for church access

Explore in two ways:

1. Pastor deaths

- SBC churches use single pastor for leadership
- 1-1 mapping from pastor deaths to church closures
- Pastor deaths o supply shifter for church access

2. Pastor convictions

- Sexual abuse in SBC church ightarrow 2019 Houston Chronicle exposé
- \downarrow religious attendance & belief after local pastor conviction
- Shock to religious institutional trust

Explore in two ways:

1. Pastor deaths

- SBC churches use single pastor for leadership
- 1-1 mapping from pastor deaths to church closures
- Pastor deaths o supply shifter for church access

2. Pastor convictions

- Sexual abuse in SBC church ightarrow 2019 Houston Chronicle exposé
- ↓ religious attendance & belief after local pastor conviction
- Shock to religious institutional trust

Shocks distinct in timing & granularity

- Both show religious disruptions shape outcomes

Preview of results

After a pastor death:

- First stage: SBC churches close \rightarrow persistent effects

- **Social**: ↓ social activity, no voting changes

- **Health**: No changes

- **Economic**: labor force participation (LFP) $\downarrow \sim 0.25 \mathrm{pp}$, unemployment $\uparrow \sim 0.25 \mathrm{pp}$

7

Preview of results

After a pastor death:

- **First stage**: SBC churches close \rightarrow persistent effects
- **Social**: ↓ social activity, no voting changes
- **Health**: No changes
- **Economic**: labor force participation (LFP) $\downarrow \sim$ 0.25pp, unemployment $\uparrow \sim$ 0.25pp

After a pastor conviction:

- **First stage**: ↓ church attendance & later ↓ affiliation
- **Social**: voting changes ($\uparrow \sim 0.5$ pp shift left)
- **Health**: ↑ opioid mortality
- **Economic**: LFP & unemployment \rightarrow same magnitude as deaths analysis

Preview of results

After a pastor death:

- **First stage**: SBC churches close → persistent effects
- **Social**: ↓ social activity, no voting changes
- Health: No changes
- **Economic**: labor force participation (LFP) $\downarrow \sim 0.25$ pp, unemployment $\uparrow \sim 0.25$ pp

After a pastor conviction:

- **First stage**: ↓ church attendance & later ↓ affiliation
- **Social**: voting changes ($\uparrow \sim 0.5$ pp shift left)
- **Health**: ↑ opioid mortality
- **Economic**: LFP & unemployment ightarrow same magnitude as deaths analysis

Hedonic demand: WTP >\$3,000 for church proximity (1 mi.) \rightarrow 80% of pref. from non-employment factors

Related literature

1. Religion & social/economic outcomes

- Economic outcomes: Weber (1905), Gruber (2005), McCleary and Barro (2006), and Campante and Yanagizawa-Drott (2015)
- Health outcomes and "deaths of despair": Gruber and Hungerman (2008), Case and Deaton (2015), Case and Deaton (2021), and Giles, Hungerman, and Oostrom (2023)
- Religious outcomes: Bottan and Perez-Truglia (2015)
- \rightarrow Novel granular variation + focus on large denomination

Related literature

1. Religion & social/economic outcomes

2. Social capital & labor markets

- Granovetter (1973), Topa (2001), Calvo-Armengol and Jackson (2004), Pallais and Sands (2016), Chetty et al. (2022a), Chetty et al. (2022b), and Chetty et al. (2024)
- → Explore shocks to social capital in new setting

Related literature

1. Religion & social/economic outcomes

2. Social capital & labor markets

- 3. Religion & social connection as place-based amenities
 - Valuing place-based amenities: Rosen (1974), Bajari and Benkard (2005), Chay and Greenstone (2005), Greenstone and Gallagher (2008), and Linden and Rockoff (2008)
 - Determinants of place-based amenities: Diamond (2016) and Almagro and Domínguez-lino (2024)
 - Social connection and outcomes: Putnam (2000) and Glaeser, Laibson, and Sacerdote (2002)
 - ightarrow Explicitly consider *religion* & *social connection* as place-based amenities

Outline

Background

Basic model

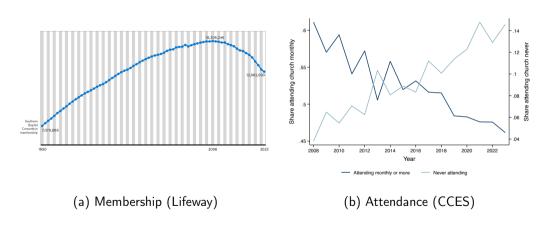
Empirical strategies & proximate outcomes

Social & economic outcomes

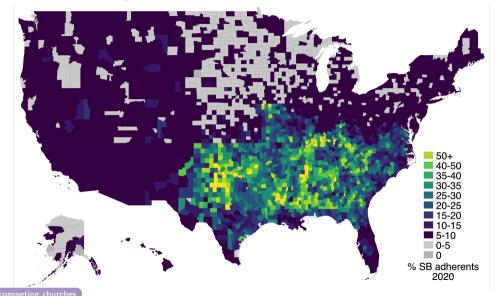
Valuing religion

SBC church trends

Membership \downarrow 20% since 2006 \rightarrow over 3 million people

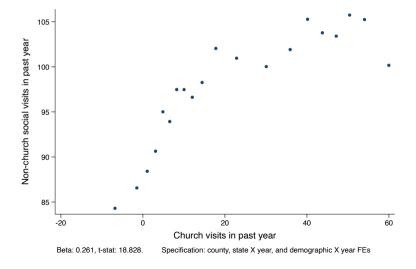


Where is the SBC present?



Church attendance and social activity

 \uparrow church visits associated with \uparrow non-church social activity



Outline

Background

Basic model

Empirical strategies & proximate outcomes

Social & economic outcomes

Valuing religion

Why should we expect religion to matter? Model three key features:

- 1. Religion as a source of social capital
- 2. Religion as an amenity
- 3. Religion as an source of norms

Why should we expect religion to matter? Model three key features:

- 1. Religion as a source of social capital
- 2. Religion as an amenity
- 3. Religion as an source of norms

Individual recieves utility from church attendance a and some other action y:

$$U(a,y) = \underbrace{\left[e(a)w + \left(1 - e(a)\right)b\right]}_{\text{attendance channel}} + \underbrace{\begin{array}{c} \text{norms channel} \\ \\ \lambda y \\ \end{array}}_{\text{norms channel}} + \underbrace{\begin{array}{c} \\ \\ \lambda y \\ \end{array}}_{\text{norms channel}}$$

Why should we expect religion to matter? Model three key features:

- 1. Religion as a source of social capital
- 2. Religion as an amenity
- 3. Religion as an source of norms

Individual recieves utility from church attendance a and some other action y:

$$U(a,y) = \underbrace{\left[\underline{e(a)w + \left(1 - e(a) \right)b} \right]}_{\text{expected income}} + \gamma a + \lambda y - \frac{1}{2} \varphi y^2$$

- Job-finding rate
$$m(a) = \underbrace{\alpha}_{\substack{\text{help-wanted} \\ \text{ads}}} + \underbrace{\beta a}_{\substack{\text{referrals}}} \implies e(a) \approx e_0 + \kappa a \text{ (networks} \to \text{jobs)}$$

Why should we expect religion to matter? Model three key features:

- 1. Religion as a source of social capital
- 2. Religion as an amenity
- 3. Religion as an source of norms

Individual recieves utility from church attendance a and some other action y:

$$U(a,y) = \left[e(a)w + \left(1 - e(a)\right)b\right] + \underbrace{\gamma a}_{\text{amenity val.}} + \lambda y \quad - \qquad \frac{1}{2}\varphi y^2$$

- Direct amenity value from church attendance, $\gamma>0$

Why should we expect religion to matter? Model three key features:

- 1. Religion as a source of social capital
- 2. Religion as an amenity
- 3. Religion as an source of norms

Individual recieves utility from church attendance a and some other action y:

$$U(a,y) = \left[e(a)w + \left(1 - e(a)\right)b\right] + \qquad \gamma a \qquad + \underbrace{\frac{\lambda y}{e^{\text{hedonic}}}}_{\text{"reward"}} - \underbrace{\frac{1}{2}\varphi y^2}_{\text{cost of deviating from church}}$$

- Norms channel ightarrow cost (governed by arphi) of actions not aligned with church values
 - Church bliss point normalized to 0: $y^* = \frac{\lambda}{\varphi} \ o \ ext{hedonic/alignment tradeoff}$

Testable implications

Pastor deaths \implies church closures: $\downarrow a$

Church abuse scandals \implies belief shock: $\downarrow a$ and $\downarrow \varphi$

Effects for both:

- 1. ↑ unemployment (networks)
- 2. ↓ labor force participation (networks)
- 3. ↓ home prices (bundled amenities + job-finding benefits)

Effects only with scandals:

1. \uparrow Norm compliance / moral adherence (\downarrow belief $\Longrightarrow \downarrow$ deviation costs)

Today: Reduced-form evidence & some decomposition

Outline

Background

Basic model

Empirical strategies & proximate outcomes

Social & economic outcomes

Valuing religion

Estimating the effects of pastor deaths: data

Scan & OCR universe of SBC pastors from 1970 to 2008

→ Pastor names & locations biannually

Merge to Social Security Death Master File & Infutor

 \rightarrow Universe of deaths & locations up to 2013

Variation in pastor deaths with exact church locations

PASTORS

Kv 40741

neva Al 36340 Aaron Marvin 3005 Sheldon Clovis NM 88101 Abanathy Charles PO Bx 97 Black Rock Ar 72415 Abbott Barney 305 E 4th Penn W Holdenville Ok 74848 Abbott Clifford E Modena Bo Ch Modena Mo 64663 Abbott Cloyd Rt 3 Tazewell Tn Abbott Don PO By 334 Forrest City Ar 72335 Abbott E A 705 No Jackson St Albany Ga 31705 Abbott Earl Rt 5 By 922 London

Aaron Joseph L Rt 1 Bx 69 Ge-

Abbott Eugene Thompsonville Il Abbott H W 3162 Pershall Rd Saint Louis Mo 63136 Abbott Ivan J 411 E Waggoner St

Sullivan Il 61951

terprise Al 36330 Abbott John B Bx B B Espanola NM 87532 Aaron Lafayette Rt 1 Cussetta Al Abbott Kenneth L 509 E Woodayd Dennison Tx 75020 Abbott Lewis 429 So Riverbills Dr

> Abbott Raymond C-26 Madison Square Apt Madison Tn 37115 Abbott Wilburn 1906 Lydia Dr Owensboro Ky 42301 Abbott Frank A Jr 1445 Downing

> St Charleston SC 29407 Abel H B Rt 1 Vance Ms 38964 Abel Harlan A 6503 W Cameron

Tulsa Ok 74127 Ridge Ar 72476

Ehrhardt SC 29081 Abel W B Noxapater Ms 39346 Abel William M PO Bx 582 Newland NC 28657

Abell Troy D Bx 117 Wheatley Ky

Temple Terrace Fl 33617

Abel Jim PO Bx 37 SBC Walnut Abel Richard St Johns Bn Ch

Abbott James 105 Bullard St En. Abercombie Alex N Collins Ms 39428 Abercombie C L 1310 No Crain Altus Ok 73521 Abercrombie C M Wheeler Tx

Abercrombie J B Bellview Bp Ch Laurens SC 29360

Abercrombie M L Rt 4 Pickens SC Abercrombie Robert M Rt 1 Bx

6236 McCalla Al 35111 Abernathy D J 741 No Mills Av Orlando Fl 32803 Abernathy Dan Rt 1 Bx 211 New London NC 28127

Abernathy Donald Rt 1 Fyffe Al Abernathy Eugene 2611 SW 13 Pl

Fort Lauderdale Pl 33312 Abernathy James W 3407 Kester Wood Dr Knoxville Tn 37918 Abernathy Jerry D 706 Pecan

Abernathy Paul J 700 Morgan Falls Rd Dunwoody Ga 30043

Abernathy Roy Rt 3 Canton Ga 30114

1970 SBC Annual

Estimating the effects of pastor deaths: regression

Exploit variation in treatment & timing \rightarrow matched controls

- Match on state, income, education, race, & church presence

$$Y_{zt} = \gamma_t + \delta_z + \sum_{k \neq -1} \beta_k PastorDeath_z \times \mathbf{1}\{t - T_z = k\} + \lambda \mathbf{X}_{zt} + \varepsilon_{zt}$$

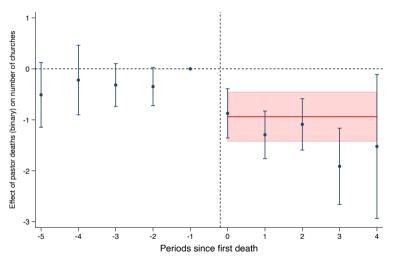
 Y_{zt} : outcome in zip code z in year t

 $t-T_z$: time from first pastor death

 β_k : effect of pastor deaths

 \mathbf{X}_{zt} : time-varying controls

Churches close when pastors die



Robust to using non-binary, non-absorbing treatment [Chaisemartin & D'Haultfœuille, 2024]

► CD estimator ► cumulative dead

Estimating the effects of pastor convictions: data

125 SBC pastor convictions for sex crimes from *The Houston Chronicle*

Abuse of Faith: The database

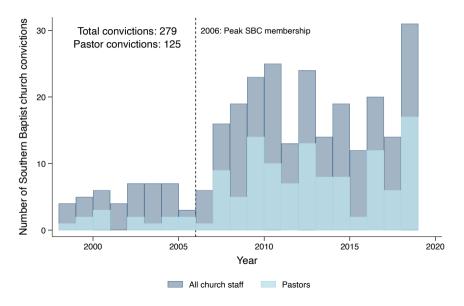
Part 1 Part 2 Part 3 Part 4 Part 5 Part 6 Database Videos



ABUSE of FAITH

In the past 20 years, hundreds of Southern Baptists with formal church roles have engaged in sexual misconduct, a new investigation by the Houston Chronicle and San Antonio Express-News reveals. They were pastors. Deacons. Youth pastors.

Timing of convictions



Estimating the effects of pastor convictions: regression

Follow same matched controls strategy as in deaths analysis

DiD with individual-level data:

$$Y_{ict} = \alpha + \delta_c + \gamma_t + \sum_{k \neq -1} \beta_k Conviction_c \times \mathbf{1}\{t - T_c = k\} + \lambda \mathbf{X}_{it} + \varepsilon_{ict}$$

 Y_{ict} : outcome for individual i in county c in year t

 $t-T_c$: time from year of conviction T_c in county c

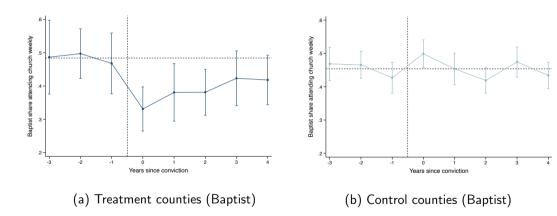
 β_k : effect of pastor conviction

 \mathbf{X}_{it} : Time-varying controls

reg with aggregate data

Baptists stop attending church after convictions

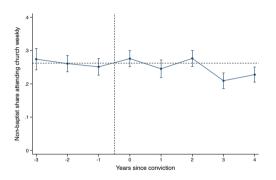
Large decline in church attendance for Baptists in treatment counties



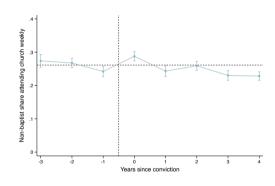
other attendance measures

Other denominations not affected

No effects for non-Baptists

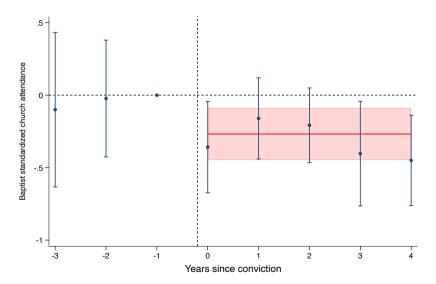


(a) Treatment counties (Non-Baptist)



(b) Control counties (Non-Baptist)

Persistent deceases in attendance



Outline

Background

Basic model

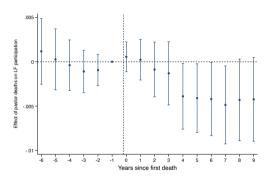
Empirical strategies & proximate outcomes

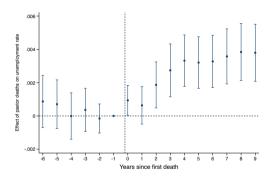
Social & economic outcomes

- 1. Pastor deaths
- 2. Pastor convictions

Valuing religion

Pastor deaths: economic outcomes LFP ↓, unemployment ↑





(a) Labor force participation

(b) Unemployment

Not driven by church employment • church employment

Pastor deaths: social effects

Table 1: Effect of pastor death on social activities

Dependent Variables:	Church visits (1)	Social visits (2)	Bowling visits (3)
$\frac{\textit{Variables}}{\log\left(\frac{\textit{PastorDead}_{zt}+0.1}{\textit{Matched}_z+0.1}\right)}$	-0.031** (0.014)	-0.014** (0.006)	-0.173*** (0.067)
Fixed effects County State \times Year Race \times Year Age group \times Year Sex \times Year City size \times Year	X X X X	X X X X	X X X X X
Fit statistics Observations Pseudo R ²	20,650 0.12	17,768 0.05	19,678 0.14

Signif. Codes: ***: 0.01, **: 0.05, *: 0.1

Outline

Basic model

Empirical strategies & proximate outcomes

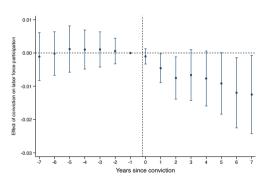
Social & economic outcomes

- 1. Pastor deaths
- 2. Pastor convictions

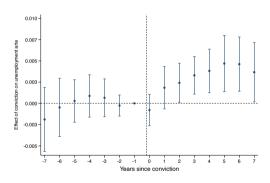
Valuing religion

Pastor convictions: economic effects

LFP \downarrow , unemployment $\uparrow \rightarrow$ same direction/magnitude as deaths analysis



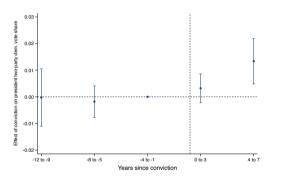
(a) Labor force participation

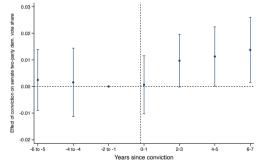


(b) Unemployment

Pastor convictions: social effects

Voting behavior \rightarrow shift left in presidential & senate elections



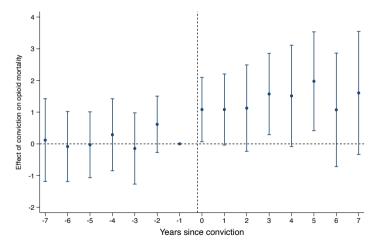


(a) Presidential vote shares

(b) Senate vote shares

Pastor convctions: deaths of despair

 $25\%\uparrow$ opioid-related mortality relative to baseline



No effects with aggregate health • aggregate deaths • pastor deaths

Outline

Background

Basic model

Empirical strategies & proximate outcomes

Social & economic outcomes

Valuing religion

Pastor deaths: home price effects of nearby churches

Can leverage exact church locations for spatial decomposition

Estimate the following with non-parametric IV:

$$\log\left(P_{jt}\right) = \underbrace{\theta\left(\delta_{jt}\right)}_{\text{Church dist}} + \underbrace{\phi\left(\delta_{j,1994}\right)}_{\text{1994 dist}} + \underbrace{\beta X_{j}}_{\text{Chars.}} + \underbrace{\gamma_{c(j)t}}_{\text{County}} + \underbrace{\zeta_{n(j)}}_{\text{Tract FEs}} + \varepsilon_{jt}$$

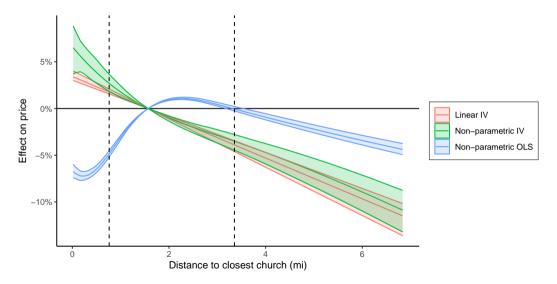
Flexibly control for pre-period distance from church with ϕ (Borusyak and Hull, 2022)

Instrument for δ_{jt} with an interaction of pre-period distance $\delta_{j,1994}$ & death timing

Estimate nonparametric effect $\hat{\theta}(\delta)$ of church distance on log home prices using NPIV (Chen and Christensen, 2018; Newey and Powell, 2003)

Sample: 7,470,446 home transactions from 1990-2008 from Corelogic

The nearest church being farther ightarrow lower home values



From price effects to preferences

Assume household i chooses housing option J_i to maximize indirect utility:

$$U_{ij} = -\beta_i \,\delta_j + U_i^{(-\delta)} \left(A_j, \eta_{n(j)} \right) + \xi_j - P_j$$

- P_i : sale price of house j
- δ_j : distance from house j to nearest SBC church
- A_j and $\eta_{n(j)}$: observed home chars. & unobserved neighborhoods chars., repsectively
- ξ_j : vertical unobserved quality of house j
- Let $X_j := \left(\delta_j, A_j, \eta_{n(j)}, \xi_j \right)$

From price effects to preferences

Assume household i chooses housing option J_i to maximize indirect utility:

$$U_{ij} = -\beta_i \,\delta_j + U_i^{(-\delta)} \left(A_j, \eta_{n(j)} \right) + \xi_j - P_j$$

Two ingredients:

- 1. Continuity: choice of housing option $j \to \text{equiv.}$ to choice of continuous house, neighborhood chars. X_j for price P_j
 - \rightarrow >7 million home transactions $\Rightarrow \approx$ continuous choice of δ_i
- 2. Bajari and Benkard (2005): no i-specific taste for particular housing options
 - \rightarrow housing option j's price $P_j =$ smooth function p of j's observed, unobserved chars.

From price effects to preferences

Assume household i chooses housing option J_i to maximize indirect utility:

$$U_{ij} = -\beta_i \,\delta_j + U_i^{(-\delta)} \left(A_j, \eta_{n(j)} \right) + \xi_j - P_j$$

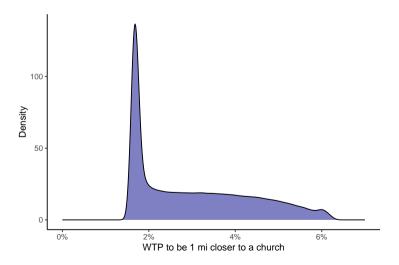
Two ingredients:

- 1. Continuity: choice of housing option $j \to \text{equiv.}$ to choice of continuous house, neighborhood chars. X_j for price P_j
 - \rightarrow >7 million home transactions $\Rightarrow \approx$ continuous choice of δ_i
- 2. Bajari and Benkard (2005): no *i*-specific taste for particular housing options
 - \rightarrow housing option j's price $P_j =$ smooth function p of j's observed, unobserved chars.
- Continuous choices of char. bundles + smooth price function $P_j = p(\delta_j, A_j, \eta_{n(j)}, \xi_j)$
 - \rightarrow Household i's FOC identifies disutility from church distance β_i



Hedonic willingness-to-pay

Dollar-denominated average WTP to be 1 mile closer to church = \$3,235

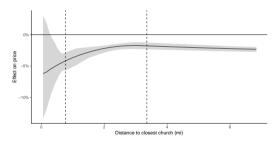


Decomposition of church value

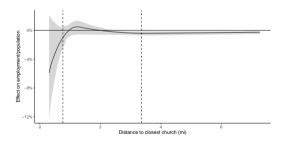
Split value of proximity into employment channel $e(\delta_j)$ and residual amenity value δ_j^r

$$-\beta_i \, \delta_j = -\alpha_i \, \delta_j^r + \gamma_i \, e(\delta_j), \qquad (\alpha_i, \gamma_i) \sim \mathcal{N}(\mu, \Sigma).$$

Differential slopes of price effects and employment effects help decompose WTP



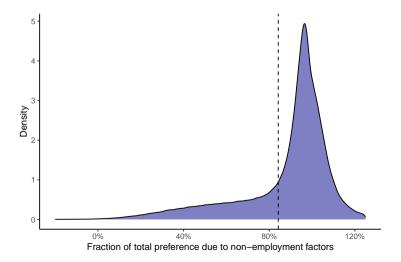
(a) Home price effects slope



(b) Employment effects slope

Employment value vs. other amenities

Over 80% of church proximity value comes from non-employment factors



Conclusion

We study effects of religion in the US with two complementary strategies

Provide framework for how religion affects outcomes \rightarrow key features:

- Religion as an amenity
- Religion as a source of social captial

Find reduced-form effects of religious loss on:

- Economic outcomes (LFP & unemployment)
- Social outcomes (social activity & voting)
- Health outcomes (opioid mortality)

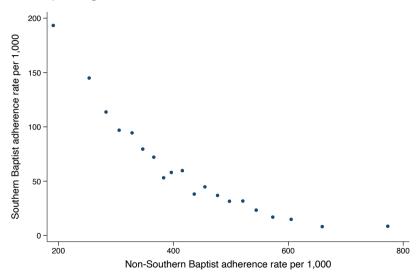
Characterize household preferences for church proximity

- Many households willing to pay to be closer to churches
- Effects come both from ↑ employment effects (20%) and other amenities (80%)

Thank you!
mpienkny@u.northwestern.edu

Appendix

Few other competing churches





Estimating the effects of pastor deaths: regression

Difference-in-differences with non-binary treatment [Chaisemartin & D'Haultfœuille, 2024]

$$Y_{zt} = \gamma_t + \delta_z + \sum_{k \neq -1} \beta_k \left[\log \left(\frac{PastorDead_{zt} + 0.1}{Matched_z + 0.1} \right) \times \mathbf{1} \{ t - T_{zt} = k \} \right] + \varepsilon_{zt}$$

 Y_{zt} : outcome in zip code z in year t

 $t-T_{zt}$: time from pastor death o allows for multiple events

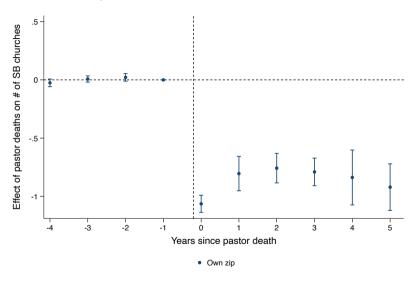
 β_k : effect of pastor deaths

Intuition: compare outcomes for "switchers" & control units with same baseline treatment status

- Estimand is AVSQ ightarrow average of actual versus status quo outcomes
- Identification comes from parallel trends conditional on baseline treatment

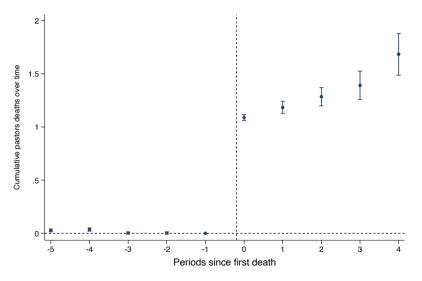
→ back

Churches close when pastors die





Cumulative deaths following first death





Estimating the effects of pastor convictions for other outcomes

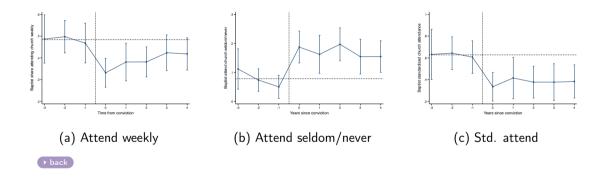
Apply same matched controls approach to aggregate outcomes

With aggregate data:

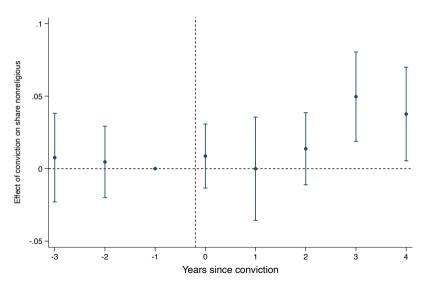
$$Y_{ct} = \delta_c + \gamma_t + \sum_{k \neq -1} \beta_k Conviction_c \times \mathbf{1}\{t - T_c = k\} + \mathbf{X}_{ct} + \varepsilon_{ct}$$

▶ back

Various measures of church attendance

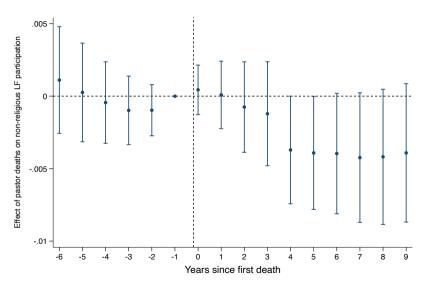


Delayed increase in non-religious share





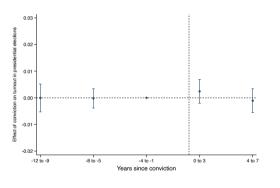
Non-church employment effects

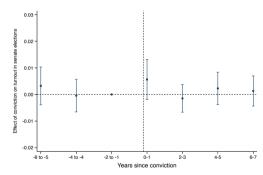




Driven by persuasion, not mobilization

No effects on turnout



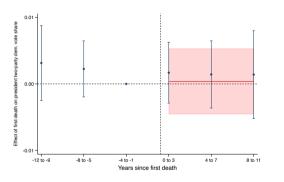


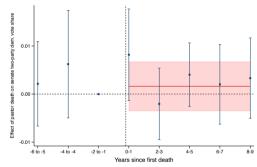
(a) Presidential election turnout

(b) Senate election turnout



No effect on voting outcomes



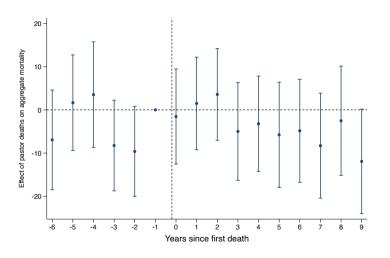


(a) Presidential vote shares

(b) Senate vote shares

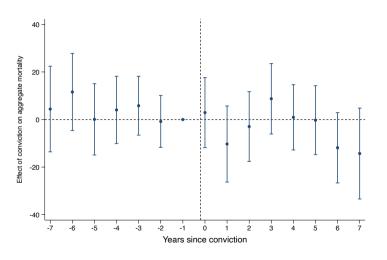
→ back

No aggregate health effects



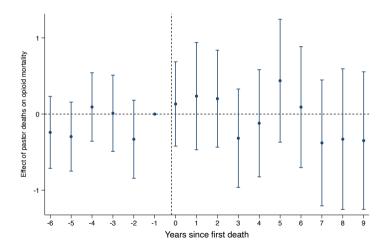


No aggregate health effects



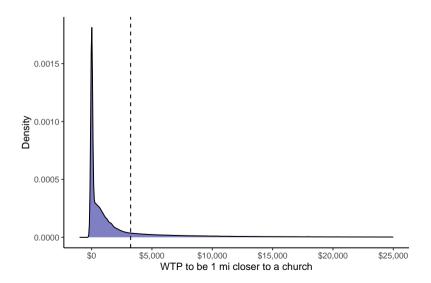


Pastor deaths: deaths of despair No change in opioid mortality



No effects with aggregate health Paggregate deaths Pack

WTP in dollars





Prices to preferences derivation

From NPIV on home prices we nonparametrically recover $\theta(\delta) = \frac{\partial \log(P)}{\partial \delta}$

Rewrite household optimization problem to be directly over bundles of housing characteristics:

$$\max_{\delta, a, \eta, \xi \in \mathcal{X}} u_i(\delta, a, \eta, \xi) - p(\delta, a, \eta, \xi), \qquad u_i(\delta, a, \eta, \xi) = -\beta_i \delta + U_i^{(-C)}(a, \eta) + \xi$$

And take the FOC:

$$\left. \frac{\partial u_i}{\partial \delta} \right|_{X_{J_i}} - \left. \frac{\partial p}{\partial \delta} \right|_{X_{J_i}} = 0 \implies \beta_i = \left. \frac{\partial u_i}{\partial \delta} \right|_{X_{J_i}} = \left. \frac{\partial p}{\partial \delta} \right|_{X_{J_i}} = p(X_{J_i}) \theta(\delta_{J_i})$$

▶ back